Section 2.3: Modeling with First Order Equations

Objectives:

- Model a real-world situation with a DE.
- Solve the DE.
- Analyze and interpret the solutions.

Example 1: Water Tank

A tank initially contains 40 pounds of salt dissolved in 600 gallons of water. Time is measured in minutes. Starting at time t = 0, water that contains 1/2 pound of salt per gallon is poured into the tank at the rate of 4 gal/min and the mixture is drained from the tank at the same rate.

- (a) Construct an IVP modeling Q(t), which is the number of pounds of salt in the tank at time t > 0.
- (b) Solve the IVP to determine an expression for Q(t).
- (c) After a long period of time, what happens to the concentration of salt in the tank?



Example 2: Population Model

The world population in 2019 was roughly 7.7 billion.

- (a) The world population is increasing at a rate of 1.1% per year. If the growth rate remains fixed at 1.1%, how long will it take for the population of the world to reach 20 billion people?
- (b) Assume the earth cannot support a population beyond 20 billion people. If the population growth rate is **also** proportional to the difference between how close the world population is to this limiting value, what is the expression that gives the world population as a function of time?