Georgia Tech - Lorraine Spring 2020
Differential Equations
Math 2552
$30 / 1 / 2020$

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| TOT |  |

## Quiz $\mathrm{n}^{0} 2(20$ minutes $)$

Show your work and justify your answers. Calculators, notes, cell phones, books are not allowed. Please do not use red or pink ink. Maximum: 20 points

Exercise 1 ( $3+3$ points) .
Classify the following differential equations as separable, linear, exact, or none of these.
Do not attempt to solve the differential equation. Justify your answers.

1. $\left(y^{2}+1\right)+(y+2 x y) \frac{d y}{d x}=0$.
2. $\left(x^{2}+y\right)+(1+2 x) \frac{d y}{d x}=0$.

Exercise $2(1+4+3+4+2$ points) . Consider the initial value problem corresponding to the linear differential equation

$$
(x-1) \frac{d y}{d x}+\frac{2 x y}{x+1}=1
$$

with initial condition $y(0)=1$.
(a) Write the differential equation in standard form.
(b) Determine the largest interval $I$ where the solution of the initial value problem exists and is unique. Justify your answer.
(c) Find an integrating factor for the differential equation.
(d) Find the general solution of the differential equation.
(e) Find the solution of the given initial value problem.

