Georgia Tech – Lorraine Spring 2020 Differential Equations Math 2552 30/1/2020

Last Name: First Name: EX 1 2 TOT

Quiz n^0 2 (20 minutes)

Show your work and justify your answers. Calculators, notes, cell phones, books are not allowed. Please do not use red or pink ink. Maximum: 20 points

Exercise 1 (3+3 points).

Classify the following differential equations as separable, linear, exact, or none of these. Do not attempt to solve the differential equation. Justify your answers.

1.
$$(y^2 + 1) + (y + 2xy)\frac{dy}{dx} = 0.$$

2.
$$(x^2 + y) + (1 + 2x)\frac{dy}{dx} = 0.$$

 $Exercise\ 2\ (1+4+3+4+2\ points)$. Consider the initial value problem corresponding to the linear differential equation

$$(x-1)\frac{dy}{dx} + \frac{2xy}{x+1} = 1$$

with initial condition y(0) = 1.

- (a) Write the differential equation in standard form.
- (b) Determine the largest interval I where the solution of the initial value problem exists and is unique. Justify your answer.
- (c) Find an integrating factor for the differential equation.

(d) Find the general solution of the differential equation.

(e) Find the solution of the given initial value problem.